

Exercise 1:

From a population with a mean of 400 and a variance of 1600, a random sample of 35 was taken.

(a) What is the probability that the sample mean is greater than 412?

Solution:

Given $\mu = 400$, $\sigma = \sqrt{1600} = 40$, $n = 35$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{412 - 400}{\frac{40}{\sqrt{35}}} = 1.775$$

$$P(X > 412) = P(z > 1.775) = 0.0379$$

Answer: 0.0379

(b) What is the probability that the sample mean is between 393 and 407?

Solution:

Given $\mu = 400$, $\sigma = \sqrt{1600} = 40$, $n = 35$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{393 - 400}{\frac{40}{\sqrt{35}}} = -1.035$$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{407 - 400}{\frac{40}{\sqrt{35}}} = 1.035$$

$$P(393 < X < 407) = P(-1.035 < z < 1.035) = 1 - 2 * P(z < -1.035) = 1 - 2 * 0.1503 = 0.6994$$

Answer: 0.6994

(c) What is the probability that the sample mean is less than 389?

Solution:

Given $\mu = 400$, $\sigma = \sqrt{1600} = 40$, $n = 35$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{389 - 400}{\frac{40}{\sqrt{35}}} = -1.627$$

$$P(X < 389) = P(z < -1.627) = 0.0519$$

Answer: 0.0519

Exercise 2:

A company that produces breakfast cereals packages them in boxes of 200 grams with a standard deviation of 6 grams. The population distribution of box weights is normal. Whether buy 4 boxes that can be considered a MAS be all that produced.

(a) What is the probability that average weight of these 4 boxes is less than 197?

Solution:

Given $\mu = 200$, $\sigma = 6$, $n = 4$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{197 - 200}{\frac{6}{\sqrt{4}}} = -1$$

$$P(X < 197) = P(z < -1) = 0.1587$$

Answer: 0.1587

(b) What is the probability that average weight is greater than 206?

Solution:

Given $\mu = 200$, $\sigma = 6$, $n = 4$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{206 - 200}{\frac{6}{\sqrt{4}}} = 2$$

$$P(X > 206) = P(z > 2) = 0.0228$$

Answer: 0.0228

(c) What is the probability that average weight is between 195 and 205?

Solution:

Given $\mu = 200$, $\sigma = 6$, $n = 4$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{195 - 200}{\frac{6}{\sqrt{4}}} = -1.67$$

$$z = \frac{x - \mu}{\sigma/\sqrt{n}} = \frac{205 - 200}{\frac{6}{\sqrt{4}}} = 1.67$$

$$P(195 < X < 205) = P(-1.67 < z < 1.67) = 1 - 2 * P(z < -1.67) = 1 - 2 * 0.0475 = 0.905$$

Answer: 0.905

