

$$\int \vec{F} \cdot d\vec{r} \quad \vec{F} = (-2 \sin x, -2 \cos y, xz)$$

$$\vec{r}(t) = (\underbrace{2t^3}_x, \underbrace{-t^2}_y, \underbrace{-3t}_z) \quad t = 0 \text{ to } 1$$

$$d\vec{r} = (6t^2, -2t, -3) dt$$

$$\vec{F}(t) = (-2 \sin(2t^3), -2 \cos(-t^2), -6t^4)$$

$$\begin{aligned} \vec{F} \cdot d\vec{r} &= (-2 \sin(2t^3), -2 \cos(-t^2), -6t^4) \cdot (6t^2, -2t, -3) dt \\ &= (-12t^2 \sin(2t^3) + 4t \cos(-t^2) + 18t^4) dt \end{aligned}$$

Do each term individually

$$\textcircled{1} \int -12t^2 \sin(2t^3) dt = \int_0^1 -4 \sin(t^3) dt^3 = 4 \cos t^3 \Big|_0^1$$

$$\textcircled{2} \int 4t \cos(-t^2) dt = \int 2 \cos(t^2) dt^2 = 2 \sin(-t^2) \Big|_0^1$$

$$\textcircled{3} \int 18t^4 dt = \frac{18}{5} t^5 \Big|_0^1 = 18/5$$

$$\textcircled{1} = 4 [\cos(1) - 1] \quad \textcircled{2} = 2 \sin(-1) = -2 \sin(1)$$

$$\text{Total} = 4(\cos(1) - 1) - 2 \sin(1) + \underline{18/5} \quad 3.6$$

$$(\cos(1) = 0.5403 \quad \sin(1) = \cancel{0.8415} \quad 0.8415)$$

$$4(0.5403 - 1) - 2(0.8415) + 3.6 =$$

$$-1.8388 - 1.6830 + 3.6 = 0.0782$$